

# Optimization of refueling processes in metal-hydride based hydrogen storage systems

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# We developed models based on experimental data to enable the development of a new H<sub>2</sub> storage system

## **Sandia and GM partnered to develop enabling technology for automotive H<sub>2</sub> storage systems based on solid sorbents:**

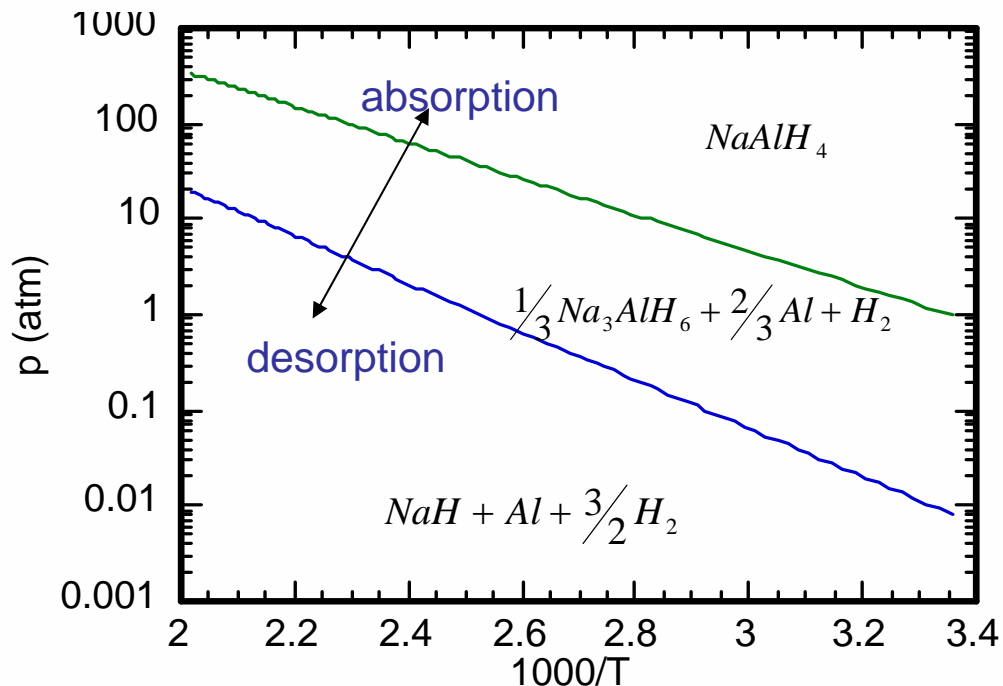
- **System drive-cycle simulation**
- **Structural design**
- **Heat and mass transfer design**
- **Prototype demonstration**

## **Goal of this presentation is two-fold:**

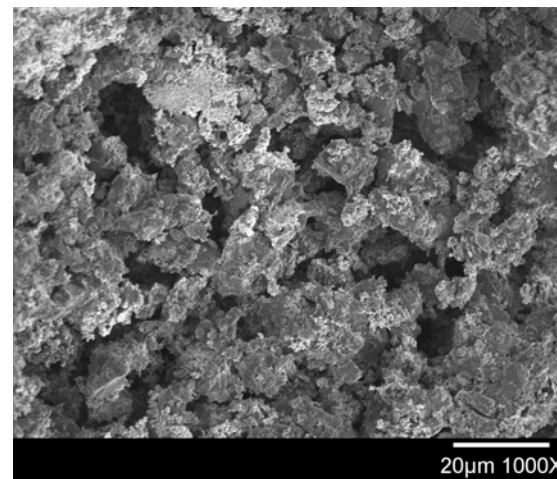
- Describe the model development process for coupled heat transfer, mass transfer, and chemical kinetics
- Demonstrate the use of these models for optimization of transportation systems.

# Catalyzed sodium alanates are prototypical reversible complex hydride materials

Van 't Hoff diagram (equilibrium P vs. T)



Significant changes occur:  
-Physical properties ( ,  $k_{th}$ , etc)  
-Morphology, porosity  
-Reactivity

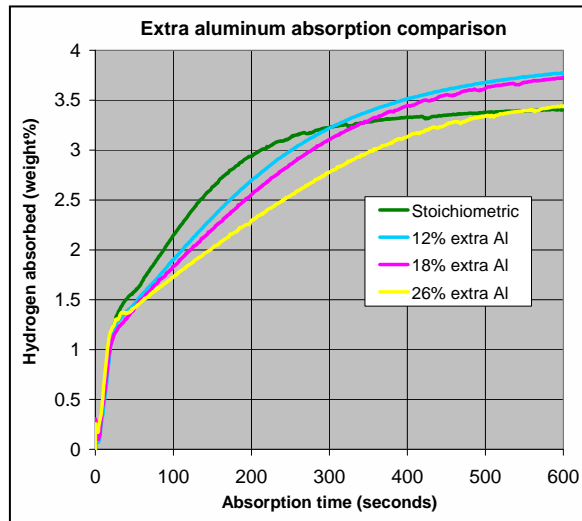


- Hydrogen uptake is exothermic (-40 kJ/mol-H<sub>2</sub>)
- Hydrogen release is equally (opposite) endothermic
- Characteristics are similar for other H<sub>2</sub> storage materials

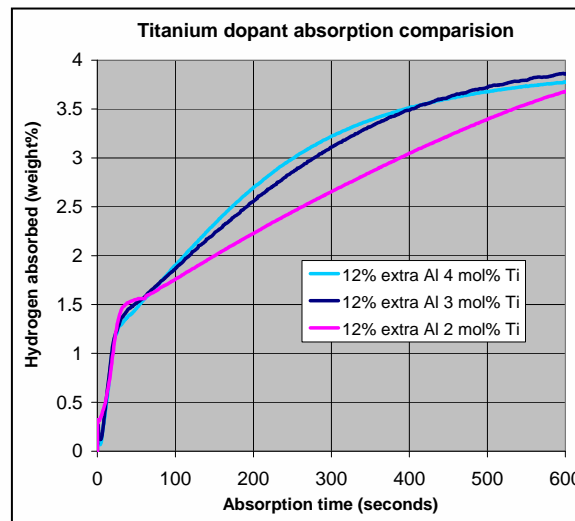
# Material properties are modified to optimize the 5 and 10 min hydrogen refill

- *Stoichiometric sodium alanates have **poor kinetics and thermal conductivity***
- *However, optimization is possible*

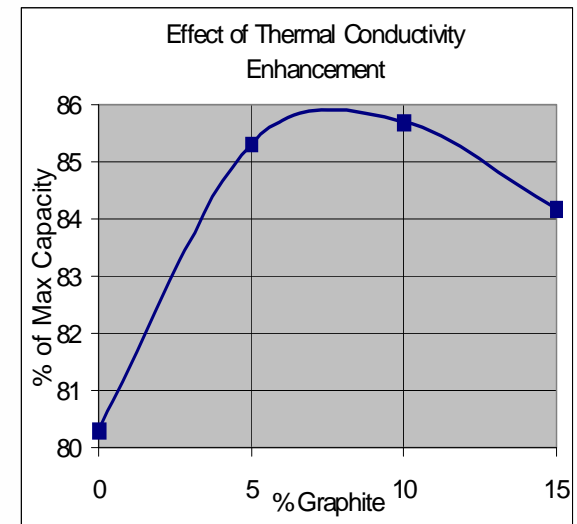
## Excess Aluminum



## Catalyst loading



## Graphite flake



## Optimized sodium alanate formulation:

- 10 wt% ENG flake
- 18 wt% excess aluminum

US Patent Pending 20070178042,  
'Sodium Alanate Hydrogen Storage Material'

# The models include momentum, species, and energy transport with chemical reactions

Momentum transport (Brinkman-Forchheimer equation):

$$\frac{\rho \partial \mathbf{v}}{\phi \partial t} + \frac{\rho}{\phi} \mathbf{v} \cdot \nabla \mathbf{u} = -\nabla p + \nabla \cdot \left[ \frac{\mu}{\phi} (\nabla \mathbf{v} + \nabla \mathbf{v}^T) \right] - \frac{\mu}{K} \mathbf{v} - \frac{\rho F}{\sqrt{K}} |\mathbf{v}| \mathbf{v}$$

Darcy term

Forchheimer term

Superficial velocity (Darcy velocity):  $\mathbf{v} = \phi \mathbf{u}$   
 $\mathbf{u}$  is the seepage velocity (intrinsic velocity)  
 $K$  is the permeability  
 $\phi$  is porosity

Energy transport:

$$(\rho c_p)_m \frac{\partial T}{\partial t} + (\rho c_p)_g \mathbf{v} \cdot \nabla T = k_m \nabla^2 T + R \Delta H$$

Species transport:

$$\frac{\partial c_i}{\partial t} + \nabla \cdot (v_i c_i) = R_i$$

Mass continuity:

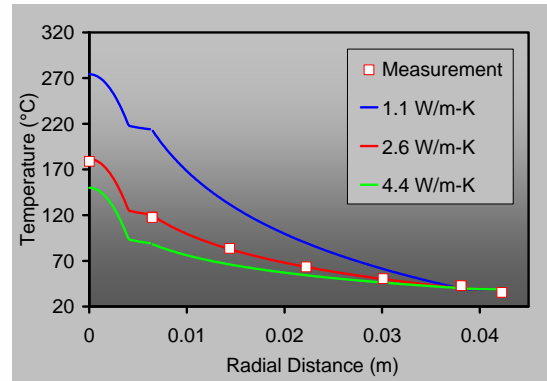
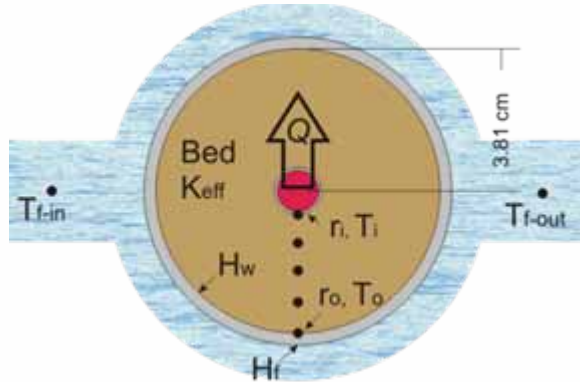
$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = MR$$

Closure is accomplished empirically

Exchange of mass between gas and solid phases

# Heat Transfer properties were experimentally optimized and quantified

Experimental apparatus:



FE model parameter fit  
for  $K_{th}$  and wall  
resistance

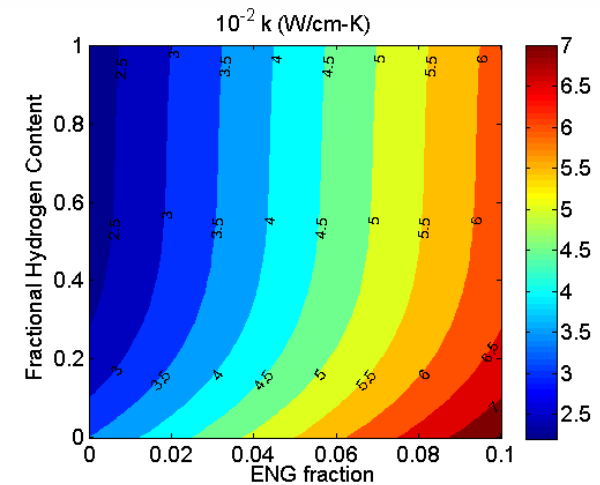


Thermal conductivity  
measured as a function of

- $H_2$  pressure
- ENG content
- $H_2$  content

Empirical formula for  $K_{th}$ :

$$k(\psi, E) = 11.7\psi^4 - 32.5\psi^3 + 33.2\psi^2 - 14.8\psi + 40E + 3.4$$



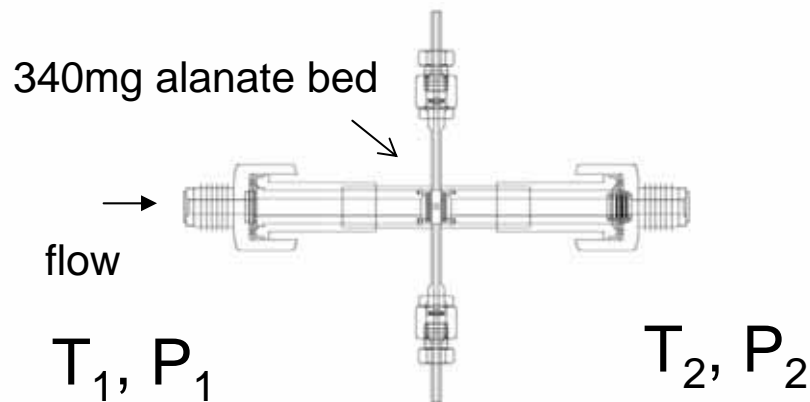
# Mass Transfer permeability (K) model chosen based on flow regimes found in a typical metal hydride bed

## Permeability model

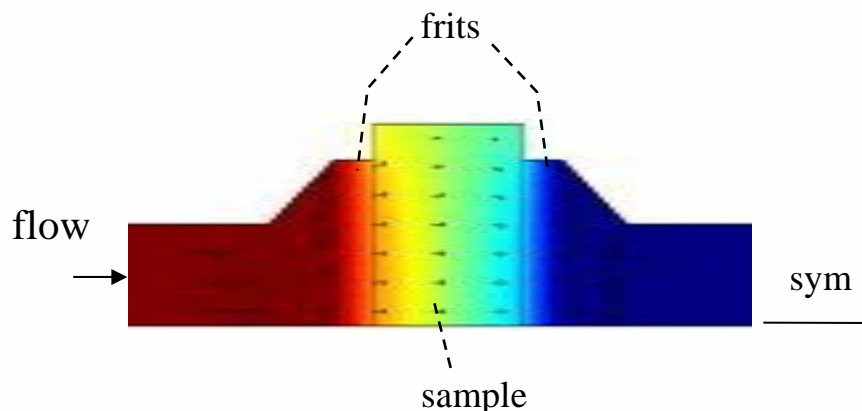
We use a model by Young & Todd that includes Knudsen number effects due to the small particle and pore sizes that characterize some materials:

$$K = \frac{\phi}{\tau^2} d_p^2 \left[ \frac{1}{32} + \frac{5}{12} Kn \right]$$

## Experimental measurement



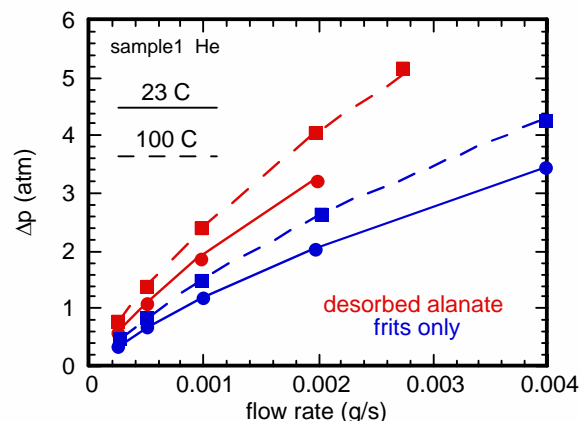
## FEM model parameter fit



## Results

Permeability model parameters:

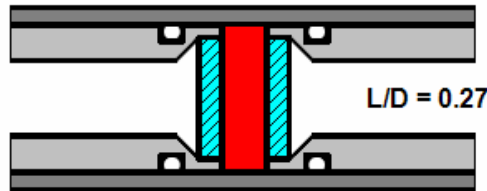
$\phi = 0.806$   
 $d_p = 3 \mu\text{m}$   
 $\tau = 2$



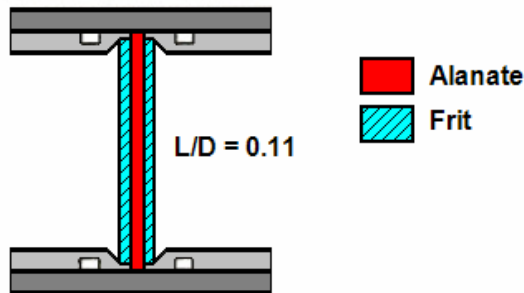
# A channeling model was developed by considering additional experimental geometries

Three aspect ratios targeted to elucidate channeling:

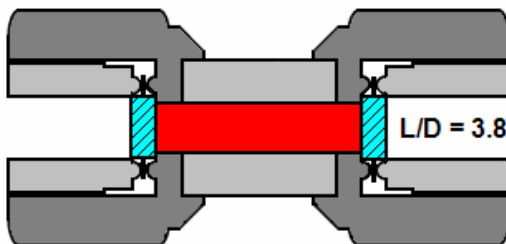
“Standard” aspect ratio



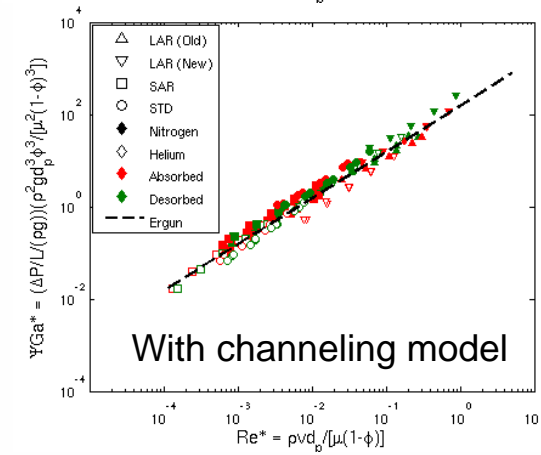
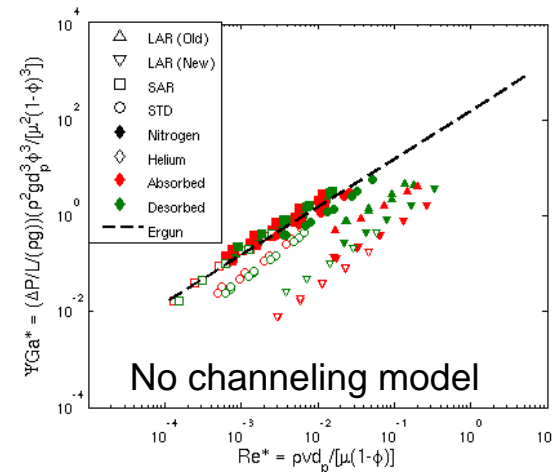
“Short” aspect ratio



“Long” aspect ratio



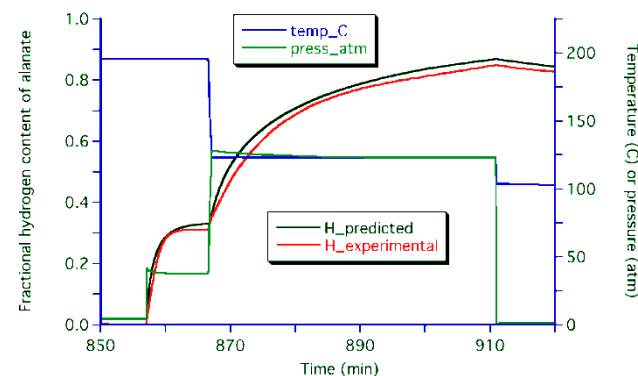
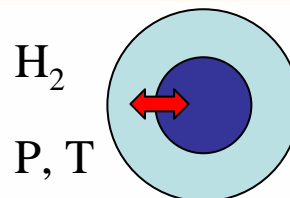
Non-dimensional pressure vs flow:



**Wall channeling model of 2.08% of total cross-sectional area found to be appropriate**

# Chemical kinetics model parameters determined using experimental measurement

- Modeled as a shrinking core with the reaction occurring at the moving interface
- Model parameters are empirically derived on small samples to exclude transport limitations
- The experimental data is fit with Arrhenius expressions
- Model parameters verified to have general applicability over entire range of operating conditions



$$R_i = f_i (p_{eq-i} - p_{H_2}) A_i e^{\frac{-E_i}{RT}} \quad \frac{\partial [H_2]}{\partial t} = \sum R_i \quad q = -\sum Q_i R_i$$

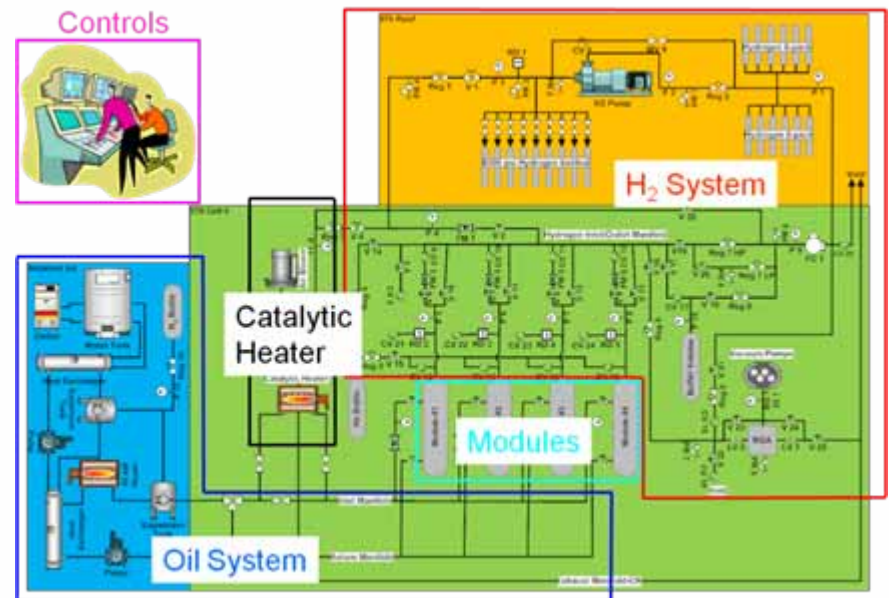
process	reaction, $i$	$f_i$	$p_{eq-i}(T)$
desorption	1	[NaAlH <sub>4</sub> ]	tetrahydride
desorption	2	[Na <sub>3</sub> AlH <sub>6</sub> ]	hexahydride
absorption	3	[NaH]	hexahydride
absorption	4	[Na <sub>3</sub> AlH <sub>6</sub> ] <sup>2</sup>	tetrahydride

# Validation at the automotive scale



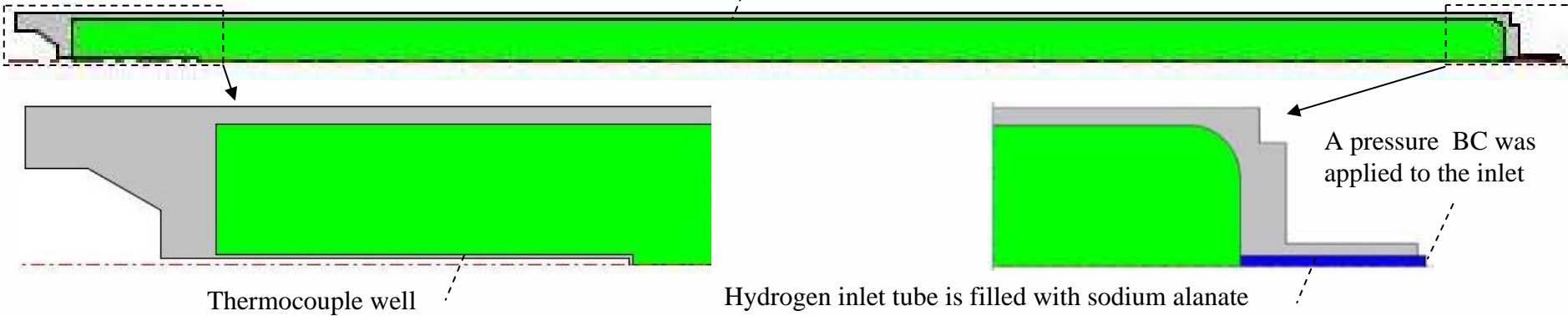
## Extensive data collection:

- Pressure, mass flow
- 18 total external shell thermocouples
- 48 thermocouples installed into end caps
- 26 RTDs on tube surfaces

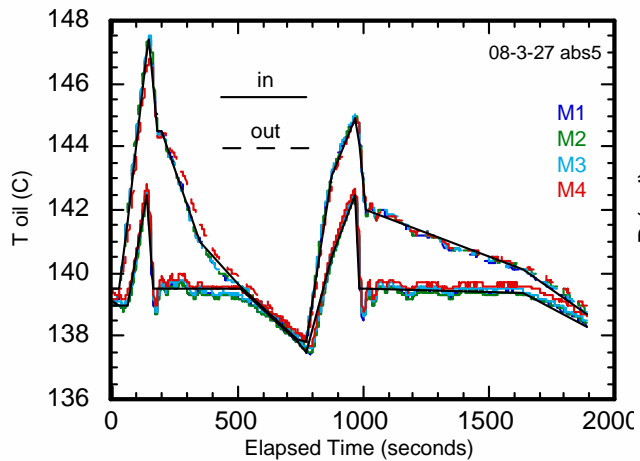


# A FE model of a module tube was constructed

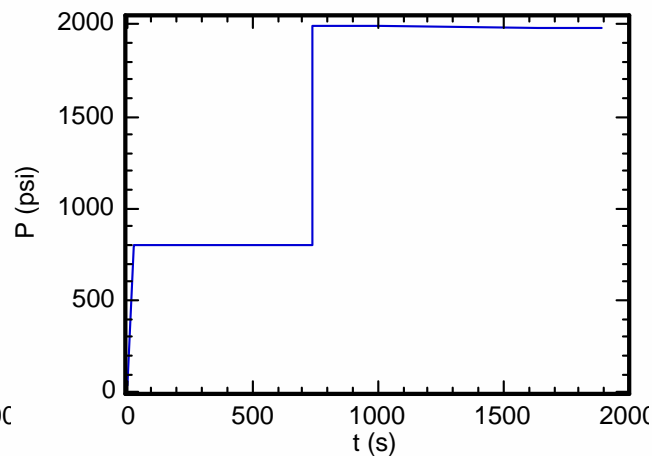
A convection bc was applied to the outer tube surface:  $q = h(T_{oil} - T)$ ;  $h = 0.065w/cmK$ ,  $T_{oil}(t,z)$



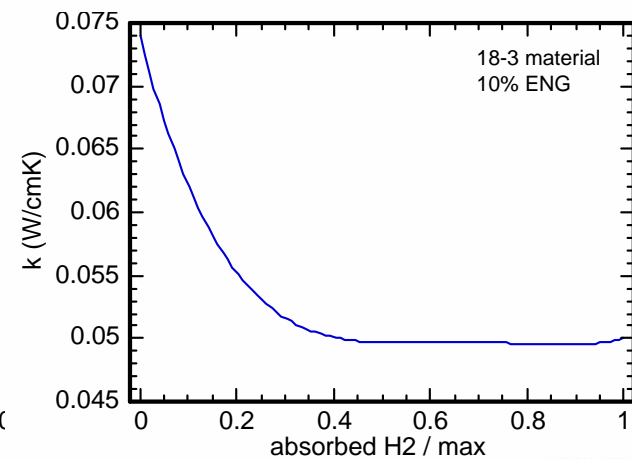
$T_{oil}$  based on measurement



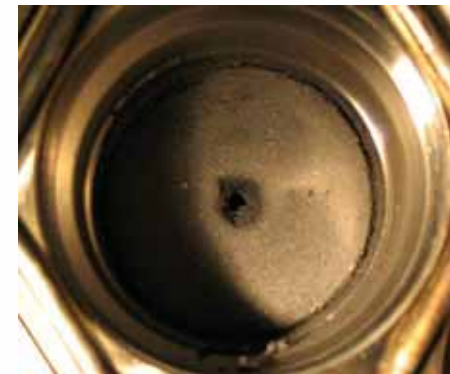
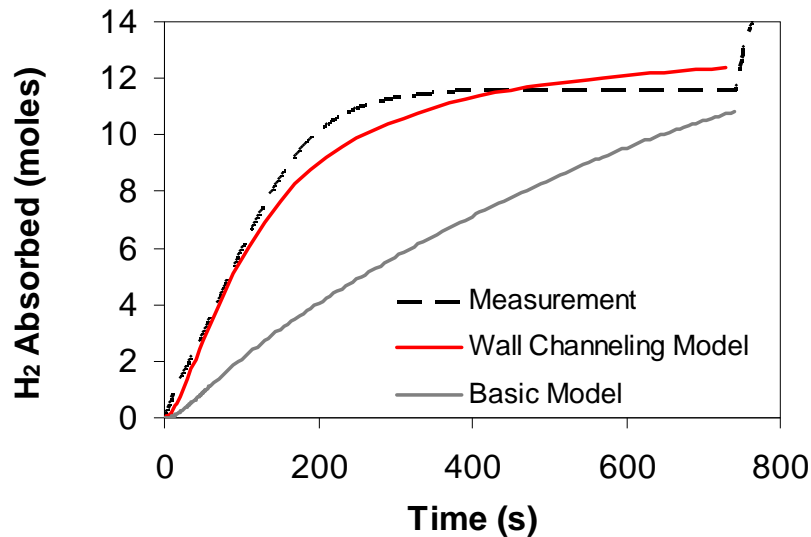
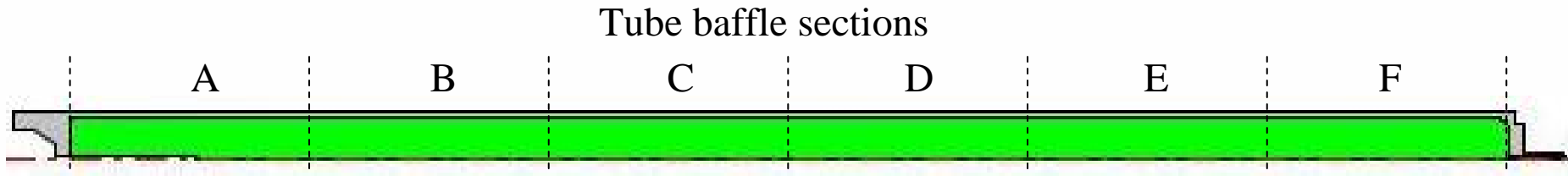
Pressure boundary condition based on measurement



Empirical alanate conductivity model



# Permeability model with channeling applied to full scale measurement



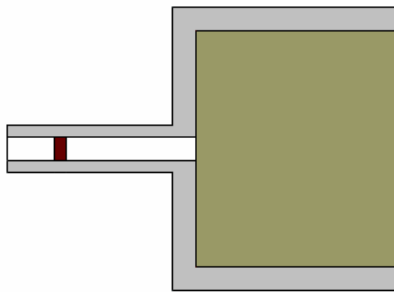
Some evidence of wall channel observed

Wall channeling model accounts for apparent high permeability in full scale system

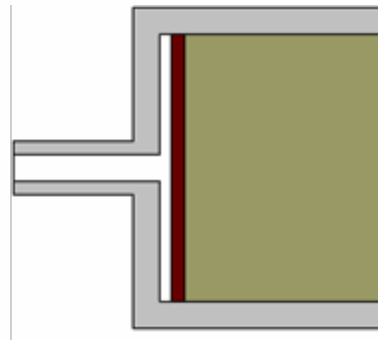
# Validated transport model enables optimization

Example of three design cases considered:

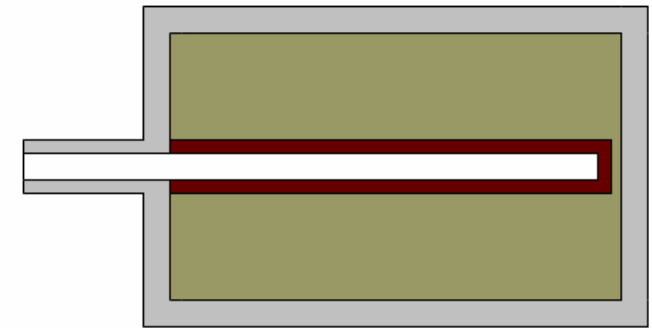
Baseline



Entry plenum



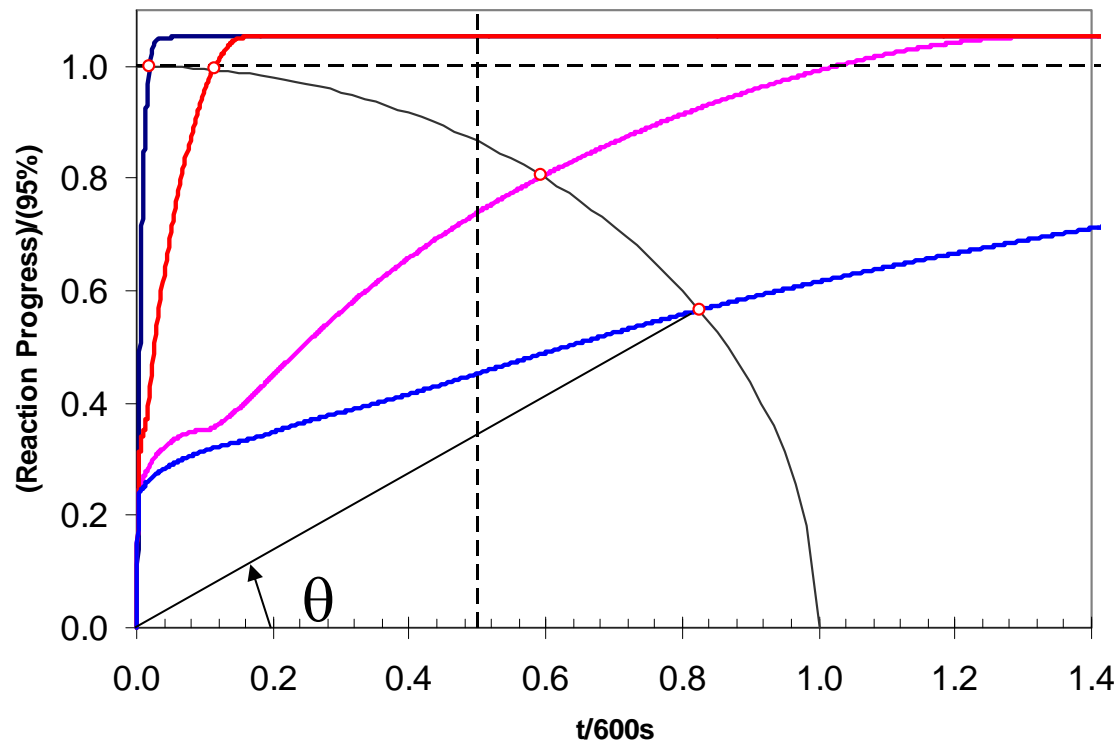
Axial Frit



# A reaction progress evaluation metric is useful to evaluate design options

## Angular position leaving normalized unit circle

Consider the 2 step sodium alanate absorption process:

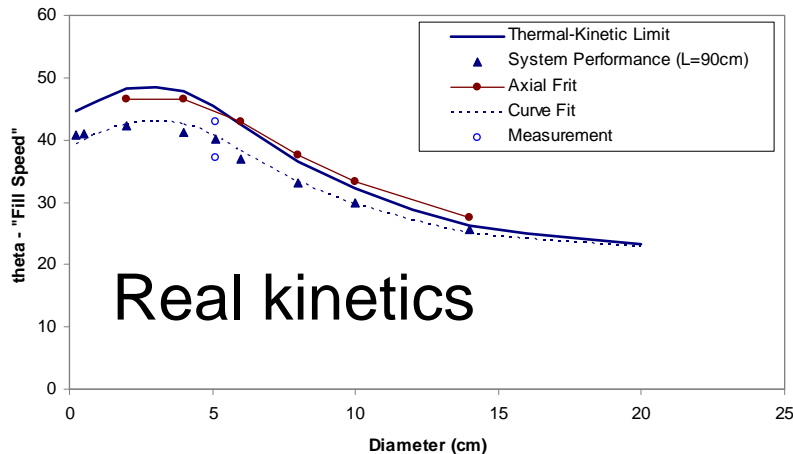


# The theoretical performance of the axial frit design approaches the thermal kinetic limit

*The thermal/kinetic limit (TKL) represents the maximum fill speed possible*

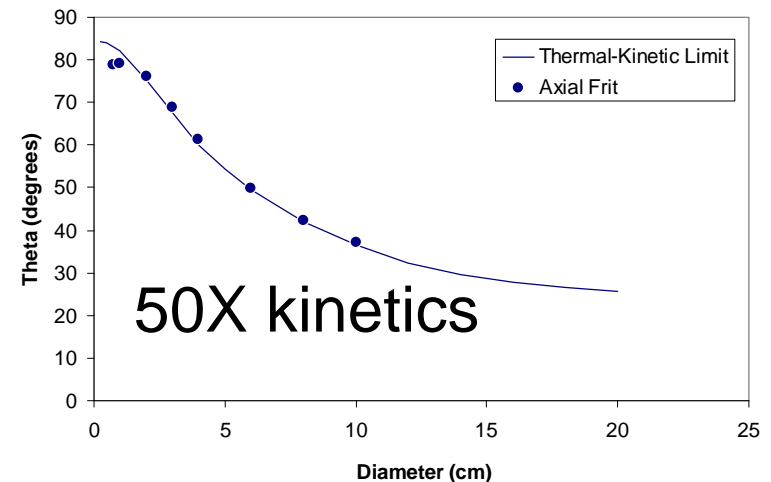
## Case 1 - Real sodium alanate kinetics:

- The axial frit design enables a 10% improvement in fill speed
- At larger diameters, the axial frit design exceeds TKL due to added cooling



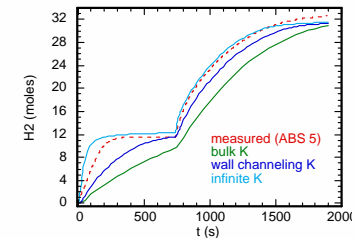
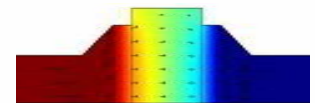
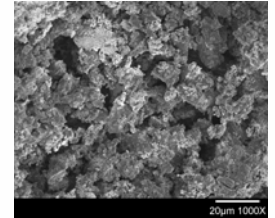
## Case 2 - Theoretical kinetics (50X):

- Sodium alanates with enhanced kinetics (50X) and existing thermal properties
- The use of the axial frit allows performance to reach the TKL



# Conclusions

- Robust model of transport in an enhanced sodium alanate system has been developed
- We have resolved the individual transport mechanisms and their impact on the rate of hydrogen uptake
- Channeling along the wall of the vessel appears to be a dominant hydrogen gas transport mechanism
- The model can be used to optimize transport and can lead to near ideal hydrogen absorption and delivery rates in scaled-up systems
- The application of these transport models is generally applicable to a variety of condensed-phase hydrogen sorption materials





# Acknowledgements

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